Note

## AN INTEGRAL SCHEME FOR THE THERMOANALYTICAL STUDY OF TWO-STEP REACTIONS

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Consider the simplest two-step reactions proceeding in monomolecular steps: parallel monomolecular reactions  $A \rightarrow B$ ;  $A \rightarrow C$ ; simultaneous independent monomolecular reactions  $A \rightarrow B$ ,  $C \rightarrow D$ ; two-step consecutive reactions; reactions involving monomolecular steps  $A \rightarrow B \rightarrow C$ . In earlier studies [1, 2], technique has been suggested for recognizing the reaction steps, identification of reaction types and determining the kinetic parameters of separate steps from the basic thermoanalytical data for thermogravimetric and scanning calorimetric analyses. However, the approach in [1] for reactions of this type has some disadvantage when applied to independent and consecutive reactions: it requires the second-order derivatives for the amount of heat released or a change in the mass  $\ddot{q}$ ,  $\dot{m}$ , which can affect the accuracy of results obtained by this method. The present study deals with a calorimetric isothermal thermoanalytical experiment which was used to develop an integral scheme not subject to such limitations in the determining of the kinetic parameters for separate steps. In this scheme,  $\int dt$  is used instead of  $\ddot{a}$ .

The rates of heat release at separate monomolecular steps are described by the following relations

$$q_1 = a + bq_1 + cq_2 = c + cq + (b - c)q_1$$

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$$\dot{q}_2 = d + fq_1 + lq_2 = d + lq + (f - l)q_1$$

$$\dot{q} = \dot{q}_1 + \dot{q}_2 = (a + d) + (c + 1)q + (b + f - c - 1)q_1$$
(1)

where  $\dot{q}$  and q are the experimentally determined rates of heat release and the total heat released (absorbed). Expressing  $q_1$  of the last equations from (1) as  $\dot{q}$  and q and substituting it into the first equation (1) we integrate it over the time and obtain the final relationship

$$\dot{q} + (la - fa + bd - cd)t - (l + b)q + (bl - cf)\int qdt - (a + d) = 0$$
(2)

For the case of two concurrent monomolecular reactions  $a = A_0B_1Q_1$ ;  $b = -B_1$ ;  $c = -(Q_1/Q_2)B_1$ ;  $d = A_0B_2Q_2$ ;  $f = -(Q_2/Q_1)B_2$ ;  $l = -B_2$ , where  $Q_i$ are the thermal effects from the steps;  $A_0$  is the number of moles of the starting material,  $B_i = K_i \exp(-E_i/RT)$  are the reaction rates at separate steps ( $K_i$  are the preexponential factor,  $E_i$  are the activation energies at separate steps). In this case eq. (2) takes up the form:

$$\dot{q} = A_0 \left( Q_1 B_1 + Q_2 B_2 \right) - (B_1 + B_2) q$$
 (3)

A scheme for determining  $K_i$ ,  $E_i$  from this relation is given in [1].

In case of independent reactions  $a = A_0B_1Q_1$ ;  $b = -B_1$ ; c = f = 0;  $d = D_0B_2Q_2$ ;  $l = -B_2$ ; and for the consecutive reactions  $a = A_0B_1Q_1$ ;  $b = -B_1$ , c = d = 0; ;  $f = -(Q_2/Q_1)B_2$ ;  $l = -B_2$  and for reactions of these two types (2) can be expressed as

$$\frac{\dot{q}_{0} - \dot{q}}{q} = (B_{1} + B_{2}) - B_{1}B_{2} = \frac{q_{\infty t} - \int qdt}{q}$$
(4)

Here  $q_{\infty}$  is the experimentally determined total amount of the released (absorbed) heat. For the independent reactions  $q_{\infty} = A_0Q_1 + D_0Q_2$ ; for the consecutive reactions,  $q_{\infty} = A_0 (Q_1 + Q_2)$ . The term  $\dot{q}_0$  is the rate of heat evolution at the initial moment of time (the moment at which the experimental temperature is attained). Further steps to be taken to identify these types of reactions and to determine the constants for separate steps from eq. (4) are given in [1]. It should be noted that with  $\dot{q}_0$  and  $q_{\infty}$ , the kinetic parameters can be determined with the values of  $Q_i, A_0, D_0$  not known. The present scheme can also be used in a gravimetric thermoanalytical experiment as well as for non-isothermal conditions, particularly if the experiment involves successive stepwise heating of the sample, with the entire temperature range covered during one run. Heating of this type is believed to be most preferable for thermal analysis, insofar as the nonisothermal experiment proceeds mainly under the "quasiisothermal" conditions, most convenient for the kinetic treatment.

## References

- 1 N. I. Vaganova, V. I. Rosenband and V. V. Barzykin, J. Thermal Anal. 34 (1988) 73.
- 2 N. I. Vaganova, V. I. Rosenband and V. V. Barzykin, J. Thermal Anal. 34 (1988).